## Abington Heights School District Geometry Accelerated Curriculum



In Geometry Accelerated, students develop their numeracy skills through the following areas of study:

1. Congruence, Similarity, and Proofs
2. Coordinate Geometry and Right Triangles
3. Properties of Polygons and Polyhedra
4. Properties of Circles, Spheres, and Cylinders
5. Measurements of Two-Dimensional Shapes and Figures
6. Measurements of Three-Dimensional Shapes and Figures

Board Approval Date: June 7, 2023
Adoption: 2023-2024 SY
Review Date:


## Abington Heights Math Framework

| Stakeholders | Actions |
| :---: | :---: |
| Students | $\star$ Engage in mathematical discussions, share their ideas openly, be inquisitive, seek to understand and learn more about mathematical concepts, and try their best daily. <br> $\star$ Exhibit creativity and curiosity in problem solving individually and collaboratively. <br> $\star$ Persevere in engaging and challenging daily mathematical practice. <br> $\star$ Come prepared to learn every day. |
| Teachers | $\star$ Create a safe and collaborative classroom environment where students feel vested in a shared vision for mathematical excellence. <br> $\star$ Develop high quality instruction that meets the needs of all learners through differentiation. <br> $\star$ Use a variety of 21st century methodologies to advance learning. <br> $\star$ Partner with parents and guardians to support student success. <br> $\star$ Establish a collaborative community within the building and amongst grade levels to ensure a cohesive level of instruction. |
| Building Leaders | $\star$ Deeply understand the needs of teachers, students, the instructional materials being used, programs being implemented, and the expectations for state-level assessment scores <br> - Knowledgeable about program and grade level standards <br> - Ensure consistent and equal access to high-quality instructional materials and resources, building. <br> Be partners with teachers, students and families: <br> - Provide guidance and support to the mathematical community. <br> - Understand needs of teachers, students and families. <br> $\star$ Trust the educators to make professional decisions based on program, student, and district needs. |
| Central Admin | $\star$ Effectively communicate to the school board and community specific areas of need and how to support teachers and building leaders in a quest for mathematical excellence <br> $\star$ Deeply understand the needs of teachers, students, the instructional materials being used, programs being implemented, and the expectations for state-level assessment scores <br> - Have a common metric for mathematical excellence. <br> - Ensure consistent and equal access to high-quality instructional materials and resources, district. <br> - Re-examine best practices/curriculum routinely (6 years). <br> $\star$ Support a culture of collaboration between the other stakeholder groups to maintain the standard of excellence of the Abington Heights <br> $\star$ Trust the educators to make professional decisions based on program, student, and district needs. |
| Parents/ Community | $\star$ Be a strong support system and contribute by building a positive math community for students. <br> $\star$ Encourage a positive math mindset. <br> $\star$ Have conversations with their children about school and ask what they are learning about in school. <br> $\star$ Be open, receptive to the district's ideas about student learning and reach out to teachers/school to learn more about how they can support. <br> $\star$ Trust the educators to make professional decisions based on program, student, and district needs. |
| School Board | Provide the fiscal resources to support: <br> - Highly qualified professionals for mathematics <br> - High-quality instructional materials <br> - Effective and efficient math interventions for remediation <br> - Professional development for math content and instructional practices <br> Trust the educators to make professional decisions based on program, student, and district needs. |

Geometry Accelerated Scope and Sequence

| Month | Unit | Estimated Number of Weeks |
| :---: | :---: | :---: |
| September | Tools of Geometry | 4 |
| October | Constructions | 1 |
|  | Parallel and Perpendicular Lines | 3 |
| November | Parallel and Perpendicular Lines | 1 |
|  | Congruent Triangles | 3 |
| December | Congruent Triangles | 2 |
|  | Proofs | 1 |
| January | Proofs | 3 |
| February | Relationships in Triangles | 3 |
|  | Quadrilaterals | 1 |
| March | Quadrilaterals | 3 |
|  | Similarity | 1 |
| April | Similarity | 2 |
|  | Right Triangles and Trigonometry | 2 |
| May | Right Triangles and Trigonometry | 1 |
|  | Circles | 2 |
|  | Surface Area, Volume, Probability | 2 |
| June | Final Exam Review | 1 |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tools of Geometry | How do I identify, define, and accurately relay geometric terms? <br> How do I apply algebraic strategies to solve geometric problems involving points, lines, and angles? <br> What are some of the relationships between pairs of angles? | Points, lines, and planes <br> Linear Measure <br> Distance and Midpoint <br> Angle Measure <br> Angle <br> Relationships | Identify and model points, lines, and planes <br> Identify intersecting lines and planes <br> Calculate linear measurement <br> Find union and intersection <br> Find the distance between two points <br> Find the midpoint of a segment <br> Measure and classify angles <br> Identify and use congruent angles and the bisector of an angle <br> Identify and use special pairs of angles | $\begin{aligned} & \text { CC.2.3.HS.A. } 3 \\ & \text { CC.2.3.HS.A. } 11 \end{aligned}$ | Google slides <br> Delta Math <br> Desmos activity on midpoint and distance | Homework <br> Formatives of quiz practice <br> Quiz: Naming, segment addition, midpoint \& distance formulas. <br> Quiz: Angle Measures |


| Unit | Essential Questions | Content | Skills | PA Core <br> Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tools of Geometry (continued) |  |  | Identify perpendicular lines <br> Identify and name polygons <br> Find perimeter, circumference, and area of two-dimensional figures |  |  |  |
| Constructions | How do I use a straightedge, compass and protractor to draw various lines and angles? | Straightedge, compass, protractor <br> Midpoints <br> Parallel lines <br> Perpendicular lines <br> Angle bisectors <br> Congruent angles | Draw a circle <br> Copy a segment <br> Draw the perpendicular bisector of a segment <br> Draw the line perpendicular to a line through a point on the line and not on the line <br> Draw a line parallel to a given line, through a given point <br> Draw an angle bisector | CC.2.3.HS.A. 4 | Google slides <br> Mathisfun: constructions videos <br> Hands on activities using straightedge, compass and protractor | Constructions practice worksheets <br> Quiz: <br> Constructions <br> Extra Credit: <br> Constructions |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Constructions (continued) |  |  | Draw congruent angles |  |  |  |
| Parallel and Perpendicular Lines | How do I identify and prove angle relationships that occur with parallel lines and a transversal? | Parallel lines and transversals <br> Angles and parallel lines with and without algebra <br> Systems and factoring practice for angles and parallel lines <br> Auxiliary lines (Crook problems) <br> Proving lines parallel with and without algebra | Identify the relationships between two lines or two planes <br> Name angle pairs formed by parallel lines and transversals <br> Use theorems to determine the relationships between specific pairs of angles <br> Use algebra to find angle measurements <br> Recognize angle pairs that occur with parallel lines <br> Prove that two lines are parallel | CC.2.3.HS.A. 3 CC.2.3.HS.A. 11 | Google slides <br> Desmos activity on parallel lines and transversals <br> Desmos activity on the converse of the theorems <br> Delta math | Homework <br> Delta math: solving systems review <br> Delta math: factoring review <br> Formatives of quiz practice <br> Quiz: Parallel lines and transversal angles <br> Quiz: Parallel lines converse and crook problems |


| Unit | Essential Questions | Content | Skills | PA Core <br> Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Congruent Triangles | What are the special relationships about the interior and exterior angles of triangles? <br> How do I identify corresponding parts of congruent triangles and prove triangles congruent? <br> What are the special properties of isosceles and equilateral triangles? | Classifying triangles <br> Solving for sides using algebra <br> Angles of triangles <br> Triangle angle-sum corollaries <br> Congruent triangles <br> Proving triangles congruent(SSS, SAS, ASA, AAS, HL) <br> Isosceles and equilateral triangles <br> Congruence transformations (reflection, translation, rotation) | Identify and classify triangles by angle measures <br> Identify and classify triangles by side measures <br> Identify and classify triangles by side measures <br> Apply the triangle angle-sum theorem Apply the exterior angle theorem <br> Name and use corresponding parts of congruent polygons <br> Prove triangles congruent using the definition of congruence <br> Use the SSS, SAS, ASA, AAS Postulates to test for triangle congruence | $\begin{aligned} & \text { CC.2.3.HS.A. } 1 \\ & \text { CC.2.3.HS.A. } 2 \\ & \text { CC.2.3.HS.A. } 3 \end{aligned}$ | Google slides <br> Desmos Activity: Investigating Congruent Triangles <br> Delta Math | Homework <br> Formatives of quiz practice <br> Quiz: Angles of triangles <br> Quiz: Congruent triangles, SSS, SAS, ASA, AAS, HL <br> Quiz: <br> Transformations |


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| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Congruent Triangles (continued) |  |  | Use the properties of isosceles and equilateral triangles |  |  |  |
| Proofs | How do I use deductive reasoning to reach valid conclusions? <br> How do I write proofs involving algebraic and geometric concepts? | Deductive reasoning <br> Proving algebraic statements true <br> Proving angle and triangle relationships | Identify and use basic postulates, definitions, and theorems in proofs <br> Write 2-column proofs | $\begin{aligned} & \text { CC.2.3.HS.A. } 1 \\ & \text { CC.2.3.HS.A. } 2 \\ & \text { CC.2.3.HS.A. } 3 \end{aligned}$ | Google slides <br> Delta math | Homework <br> Formatives of quiz practice <br> Quiz: Algebra and segment proofs <br> Quiz: Angle and triangle proofs |
| Relationships in Triangles | What are the special segments and points related to triangles? <br> What are the relationships between the sides and angles of triangles? | Triangle midsegment <br> Perpendicular bisectors <br> Angle bisectors <br> Radicals: simplifying, adding, subtracting <br> Radicals: multiplying <br> Pythagorean theorem | Identify and use perpendicular bisectors in triangles <br> Identify and use angle bisectors in triangles Identify and use medians in triangles <br> Identify and use altitude in triangles | CC.2.3.HS.A. 3 | Google slides <br> Delta Math <br> Hands on activity using cardstock to find the centroid of a triangle | Homework <br> Formatives of quiz practice <br> Quiz: <br> Midsegments, <br> Perpendicular bisectors, Angle bisectors, Radicals, Pythagorean theorem + Bisectors in a triangle |


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| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Relationships in Triangles (continued) |  | Triangle inequality theorem | Recognize and apply properties of inequalities to the measures of the angles of a triangle <br> Recognize and apply properties of inequalities to the relationships between the angles and sides of a triangle <br> Use the Triangle Inequality Theorem |  |  | Quiz: Triangle Inequality Theorem, Ordering sides and angles |
| Quadrilaterals | How do I find and use the sum of the measures of the interior and exterior angles of a polygon? <br> How do I recognize and apply the properties of quadrilaterals? <br> How do quadrilaterals compare to one another? | Interior angles of polygons <br> Exterior angles of polygons <br> Side angles of parallelograms <br> Proving parallelograms in the coordinate plane <br> Rectangles | Find and use the sum of the measures of the interior angles of a polygon <br> Find and use the sum of the measures of the exterior angles of a polygon <br> Recognize and apply properties of the sides and angles of parallelograms | $\begin{aligned} & \text { CC.2.3.HS.A. } 3 \\ & \text { CC.2.3.HS.A. } 11 \end{aligned}$ | Google slides Delta math | Homework <br> Formatives of quiz practice <br> Quiz: Angles of polygons and parallelograms <br> Quiz: <br> Parallelograms, rectangles, rhombi, squares, trapezoids, and kites |


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| Quadrilaterals (continued) |  | Rhombi and squares <br> Trapezoids and kites | Recognize and apply properties of the diagonals of parallelograms <br> Recognize the conditions that ensure a quadrilateral is a parallelogram <br> Prove that a set of points forms a parallelogram in the coordinate plane <br> Recognize and apply the properties of rectangles, rhombi, squares, kites and isosceles trapezoids |  |  |  |
| Similarity | How do I identify similar polygons and use proportions to solve problems? <br> How do I use scale models and drawings to solve problems? | Ratio and proportions <br> Similar polygons <br> Similar triangles <br> Parallel lines and proportional parts | Write ratios <br> Write and solve proportions <br> Use proportions to identify similar polygons | CC.2.3.HS.A. 1 <br> CC.2.3.HS.A. 3 <br> CC.2.3.HS.A. 5 <br> CC.2.3.HS.A. 6 <br> CC.2.3.HS.A. 9 | Google slides <br> Delta math | Homework <br> Formatives of quiz practice <br> Quiz: Similar figures, proving triangles similar |


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| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Similarity (continued) |  | Parts of similar triangles | Solve problems using the properties of similar polygons <br> Identify similar triangles using AA, SSS, SAS <br> Use similar triangles to solve problems <br> Use proportional parts within triangles <br> Use proportional parts with parallel lines |  |  | Quiz: Proportional parts |
| Right Triangles and Trigonometry | How do I use the pythagorean theorem? <br> What are the properties of special right triangles? <br> How do I use trigonometry to find missing measures of triangles? | Pythagorean theorem and its converse <br> Pythogorean triples <br> Special right triangles <br> Trigonometry <br> Inverse trigonometric functions | Use the pythagorean theorem and its converse <br> Use the properties of $45^{\circ}-45^{\circ}-90^{\circ}$ and $30^{\circ}-60^{\circ}-90^{\circ}$ <br> triangles <br> Find trigonometric ratios using right triangles | $\begin{aligned} & \mathrm{CC} .2 .2 . \mathrm{HS} . \mathrm{C} .9 \\ & \mathrm{CC} .2 .3 . \mathrm{HS} . \mathrm{A} .3 \\ & \mathrm{CC} .2 .3 . \mathrm{HS} . \mathrm{A} .7 \end{aligned}$ | Google slides <br> Delta math <br> Trigonometry Ratios Discovery Activity | Homework <br> Formatives of quiz practice <br> Quiz: <br> Pythagorean triples <br> Quiz: <br> Pythagorean theorem and special triangles Quiz: <br> Trigonometry |


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| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Right Triangles and Trigonometry (continued) |  | Angles of elevation and depression | Use trigonometric ratios to find angle measures in right triangles <br> Solve problems involving angles of elevation and depression <br> Use angles of elevation and depression to find the distance between two objects |  |  |  |
| Circles | What are the relationships between central angles, arcs, and inscribed angles in a circle? <br> How do I define and use secants and tangents? | Circles and circumference <br> Measuring angles and arcs <br> Arcs and chords <br> Inscribed angles <br> Tangents <br> Secants, tangents, and angle measures <br> Special segments in a circle | Solve problems involving the circumference of a circle <br> Identify central angles, major arcs, minor arcs, and semi circles, and find their measures <br> Find arc lengths | $\begin{aligned} & \text { CC.2.3.HS.A. } 3 \\ & \text { CC.2.3.HS.A. } 8 \\ & \text { CC.2.3.HS.A. } 9 \end{aligned}$ | Google slides <br> Delta math <br> Circle Theorems Discovery Activity | Homework <br> Formatives of quiz practice <br> Quiz: Intro to circles, central angles \& arcs, arc lengths |


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| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Circles (continued) |  |  | Recognize and use the relationships between arcs and chords and diameters <br> Find measures of inscribed angles. <br> Find measures of angles of inscribed polygons <br> Use properties of tangents <br> Solve problems involving circumscribed polygons <br> Find measures of angles formed by lines intersecting on, inside, or outside a circle <br> Find measures of segments that intersect in the interior or exterior of a circle |  |  |  |


| Unit | Essential Questions | Content | Skills | PA Core Standards | Activities | Assessment/ Evidence of Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Surface Area, Volume, and Probability | How can I use an object's dimensions to determine its surface area and/or volume? <br> How can I use geometric properties to determine the probability of a point lying in a specific area on a shape? | Area of Plane Figures <br> Area of a Sector <br> Area of Compound Shapes <br> Surface Area of Prisms and Cylinders <br> Volume of Prisms and Cylinders <br> Volumes of Pyramids and Cones <br> Volume and Surface Area of Spheres <br> Venn Diagrams <br> Theoretical and Experimental Probability <br> Geometric Probability | Calculate areas of plane figures <br> (Triangles, <br> Parallelograms, <br> Rectangles, <br> Squares, <br> Trapezoids, and Circles) <br> Calculate surface area and volume of rectangular prisms, cylinders, and spheres <br> Find the volume of pyramids and cones <br> Use Venn <br> Diagrams to determine complements, intersection, and union <br> Calculate the experimental and theoretical probability of an event | $\begin{aligned} & \text { CC.2.3.HS.A. } 12 \\ & \text { CC.2.3.HS.A. } 13 \\ & \text { CC.2.3.HS.A. } 14 \end{aligned}$ | Google Slides <br> Delta Math <br> Desmos Activity: Surface Area | Homework <br> Formative of quiz practice <br> Quiz: Surface Area and Volume <br> Quiz: Probability |


| Unit | Essential <br> Questions | Content | Skills | PA Core <br> Standards | ActivitiesAssessment/ <br> Evidence of <br> Learning |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Surface Area, <br> Volume, and <br> Probability <br> (continued) |  | Find the <br> probability that a <br> randomly chosen <br> point lands in a <br> shaded region |  |  |  |

## Portrait of an Abington Heights Mathematician

By the end of Geometry, students will:

| Congruence, Similarity, and Proofs | Coordinate Geometry and Right Triangles | Properties of Polygons and Polyhedra | Properties of Circles, Spheres, and Cylinders | Measurements of Two-Dimensional Shapes and Figures | Measurements of Three-Dimensional Shapes and Figures |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Identify and use properties of congruent and similar polygons or solids Identify and use proportional relationships in similar figures Write, analyze, complete, or identify formal proofs | Use the <br> Pythagorean Theorem to write and/or solve problems involving right triangles Use trigonometric ratios to write and solve problems involving right triangles Calculate the distance and midpoint between two points on a number line or on a coordinate plane Relate slope to perpendicularity and/or parallelism (limited to linear equations) <br> $\square$ Use slope, distance, and/or midpoint between two points on a coordinate plane to establish properties of a two-dimensional shape | Identify and use properties of triangles, quadrilaterals, regular polygons, pyramids, and prisms | Identify, determine, and use the radius, diameter, segment, and/or tangent of a circle Identify, determine, and use the arcs, semicircles, sectors, and/or angles of a circle Use chords, tangents, and secants to find arc measures or segment measures Identify and use the properties of a sphere and cylinder | Use properties of angles formed by intersecting lines to find measures of angles Use properties of angles formed when two parallel lines are cut by a transversal to find measures of angles Estimate and find area, perimeter, or circumference of regular, irregular , or compound figure Find the area of a sector of a circle Determine how a change in a linear dimension of a figure affects its perimeter, circumference, and area Use area models to find probabilities | Calculate the surface area of prisms, cylinders, cones, pyramids, and spheres Calculate the volume of prisms, cylinders, cones, pyramids, and spheres Determine how a change in a linear dimension of a figure affects its surface area or volume |

